

We have

$$\begin{array}{r} Y E \\ M E \times \\ \hline T T T \end{array}$$

where Y, E, M, T represent different digits.

What is $E + M + T + Y$?

By considering the units digit, we have

$$E^2 \equiv T \pmod{10}$$

E	T
0	0
1	1
2	4
3	9
4	6
5	5
6	6
7	9
8	4
9	1

So T must be 0, 1, 4, 5, 6 or 9.

IF $E = 0, 1, 5$ or 6 then $T = E$ which is not possible (numbers need to be distinct)

E	T
0	0
1	1
2	4
3	9
4	6
5	5
6	6
7	9
8	4
9	1

Check the remaining cases:

$$\begin{aligned} TTT &= T \times 111 \\ &= T \times 3 \times 37 \end{aligned}$$

$$T=1: 111 = 3 \times 37 \quad \text{NO}$$

$$T=4: 444 = 4 \times 3 \times 37 = 12 \times 37 \quad \text{NO}$$

$$T=6: 666 = 6 \times 3 \times 37 = 18 \times 37 \quad \text{NO}$$

$$T=9: 999 = 9 \times 3 \times 37 = 27 \times 37 \quad \text{YES}$$

We need the units digits of the two-digit factors to be equal, and 27×37 is

the only product above which fits this requirement.

So $T=9$ and $E=7$.

Then either $Y=2$ and $M=3$ or $Y=3$ and $M=2$.

In both cases:

$$\begin{aligned} E + M + T + Y &= 7 + 2 + 9 + 3 \\ &= \textcircled{21} \end{aligned}$$